

八十六學年度 工業工程 系(所) 工業工程 組碩士班研究生入學考試

科目 統計學

科號 3201

共 5

頁第 1 頁

*請在試卷【答案卷】內作答

1. (5%) Suppose the density function of a random variable X is given by

$$f(x) = \begin{cases} 1/(b-a) & , a < x < b \\ 0 & , \text{elsewhere} \end{cases}$$

- , then a). Write down the name of the distribution. (1%)
 b). Compute the expectation and variance of X . (3%)
 c). If $a=2$ and $b=7$, what is $P(3 < X < 5.5)$? (1%)

2. (26%) The amount of kerosene(煤油), in thousands of liters(公升), in a tank at the beginning of any day is a random amount Y from which a random amount X is sold during that day. Suppose that the tank is not resupplied during the day so that x is less than or equal to y , and assume that the joint density function of these variables is given by

$$f(x,y) = \begin{cases} 2, & 0 \leq x \leq y, 0 \leq y < 1 \\ 0, & \text{elsewhere} \end{cases}$$

- a). Find marginal density function $f(x)$ of X and marginal density function $g(y)$ of Y . (5%)
 b). Compute marginal expectation and variance of X . (5%)
 c). Find conditional density function $f(x|y)$ of $X|y$ and conditional density function $g(y|x)$ of $Y|x$. (5%)
 d). Find $P(1/4 < x < 1/2 | Y=3/4)$ (5%)
 e). Find the correlation coefficient ρ . (5%)
 f). Are X and Y independent? (1%)

3. (17%) A machine is producing metal pieces that are cylindrical in shape. A sample of pieces is taken and the diameters are 1.01, 0.97, 1.03, 1.04, 0.99, 0.98, 0.99, 1.01 and 1.03 centimeters

- a). Find a 95% confidence interval for the mean diameter of pieces from this machine, assuming an approximate normal distribution. (5%)
 b). Interpret the meaning of the result in a). (8%)
 c). Suppose the specification for diameter is 1.00 ± 0.03 cm, then compute the scrap rate (proportion that are out of specification). (4%)

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4. (15%) Fifteen adult males between the ages of 35 and 50 participated in a study to evaluate the effect of diet and exercise on blood cholesterol (膽固醇) level. The total cholesterol was measured in each subject initially, and then three months after participating in an aerobic exercise program (有氧運動) and switching to a low-fat diet. The data are

subject	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
before	265	240	258	295	251	245	287	314	260	279	283	240	238	225	247
after	229	231	227	240	238	241	234	256	247	239	246	218	219	226	233

Do the data support the claim that low-fat diet and aerobic exercise are of value in reducing blood cholesterol level? Use $\alpha = 0.05$.

5. (7%) Two different analytical tests can be used to determine the impurity level in steel alloys. Eight specimens are tested using both procedures, and the results are

specimen	1	2	3	4	5	6	7	8
test 1	1.2	1.3	1.5	1.4	1.7	1.8	1.4	1.3
test 2	1.4	1.7	1.5	1.3	2.0	2.1	1.7	1.6

Is there sufficient evidence to conclude that both test gives the same mean impurity level, using $\alpha = 0.01$.

6. (15%) In city T, it is known from past experience that the probability of selecting an adult over 50 years old with cancer is 0.02. If the probability of a doctor incorrectly diagnosing a person with cancer as not having the disease is 0.15 and the probability of correctly diagnosing a person without cancer as not having the disease is 0.90, what is the probability that a person is diagnosed as having cancer?

7. (15%) Suppose the interarrival time of jobs submitted to the server follows an exponential distribution with mean interarrival time of 3 seconds. Please find the probability of 2 or more jobs in 6 seconds.

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3401
3501
3601

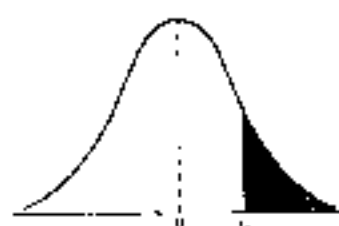


TABLE A.4 Critical Values of the *t*-Distribution

v	α						
	0.40	0.30	0.20	0.15	0.10	0.05	0.025
1	0.325	0.727	1.376	1.963	3.078	6.314	12.706
2	0.289	0.617	1.061	1.386	1.886	2.920	4.303
3	0.277	0.584	0.978	1.250	1.634	2.353	3.182
4	0.271	0.569	0.941	1.190	1.533	2.132	2.776
5	0.267	0.559	0.920	1.156	1.476	2.015	2.571
6	0.265	0.553	0.906	1.134	1.440	1.943	2.447
7	0.263	0.549	0.896	1.119	1.415	1.895	2.365
8	0.262	0.546	0.889	1.108	1.397	1.860	2.306
9	0.261	0.543	0.883	1.100	1.383	1.833	2.262
10	0.260	0.542	0.879	1.093	1.372	1.812	2.228
11	0.260	0.540	0.876	1.088	1.363	1.796	2.201
12	0.259	0.539	0.873	1.083	1.356	1.782	2.179
13	0.259	0.537	0.870	1.079	1.350	1.771	2.160
14	0.258	0.537	0.868	1.076	1.345	1.761	2.145
15	0.258	0.536	0.866	1.074	1.341	1.753	2.131
16	0.258	0.535	0.865	1.071	1.337	1.746	2.120
17	0.257	0.534	0.863	1.069	1.333	1.740	2.110
18	0.257	0.534	0.862	1.067	1.330	1.734	2.101
19	0.257	0.533	0.861	1.066	1.328	1.729	2.093
20	0.257	0.533	0.860	1.064	1.325	1.725	2.086
21	0.257	0.532	0.859	1.063	1.323	1.721	2.080
22	0.256	0.532	0.858	1.061	1.321	1.717	2.074
23	0.256	0.532	0.858	1.060	1.319	1.714	2.069
24	0.256	0.531	0.857	1.059	1.318	1.711	2.064
25	0.256	0.531	0.856	1.058	1.316	1.708	2.060
26	0.256	0.531	0.856	1.058	1.315	1.706	2.056
27	0.256	0.531	0.855	1.057	1.314	1.703	2.052
28	0.256	0.530	0.855	1.056	1.313	1.701	2.048
29	0.256	0.530	0.854	1.055	1.311	1.699	2.045
30	0.256	0.530	0.854	1.055	1.310	1.697	2.042
40	0.255	0.529	0.851	1.050	1.303	1.684	2.021
60	0.254	0.527	0.848	1.045	1.296	1.671	2.000
120	0.254	0.526	0.845	1.041	1.289	1.658	1.980
∞	0.253	0.524	0.842	1.036	1.282	1.645	1.960

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TABLE A.4 (continued) Critical Values of the t -Distribution

ν	α						
	0.02	0.015	0.01	0.0075	0.005	0.0025	0.0005
1	15.895	21.205	31.821	42.434	63.657	127.322	636.590
2	4.849	5.643	6.965	8.073	9.925	14.089	31.598
3	3.482	3.896	4.541	5.047	5.841	7.453	12.924
4	2.999	3.298	3.747	4.088	4.604	5.598	8.610
5	2.757	3.003	3.365	3.634	4.032	4.773	6.869
6	2.612	2.829	3.143	3.372	3.707	4.317	5.959
7	2.517	2.715	2.998	3.203	3.499	4.029	5.408
8	2.449	2.634	2.896	3.085	3.355	3.833	5.041
9	2.398	2.574	2.823	2.998	3.250	3.690	4.781
10	2.359	2.527	2.764	2.932	3.169	3.581	4.587
11	2.328	2.491	2.718	2.879	3.106	3.497	4.437
12	2.303	2.461	2.681	2.836	3.051	3.428	4.318
13	2.282	2.436	2.650	2.801	3.012	3.372	4.221
14	2.264	2.415	2.624	2.771	2.977	3.326	4.140
15	2.249	2.397	2.602	2.746	2.947	3.286	4.073
16	2.235	2.382	2.583	2.724	2.921	3.252	4.015
17	2.224	2.368	2.567	2.706	2.898	3.222	3.965
18	2.214	2.356	2.552	2.689	2.878	3.197	3.922
19	2.205	2.346	2.539	2.674	2.861	3.174	3.883
20	2.197	2.336	2.528	2.661	2.845	3.153	3.849
21	2.189	2.328	2.518	2.649	2.831	3.135	3.819
22	2.183	2.320	2.508	2.639	2.819	3.119	3.792
23	2.177	2.313	2.500	2.629	2.807	3.104	3.768
24	2.172	2.307	2.492	2.620	2.797	3.091	3.745
25	2.167	2.301	2.485	2.612	2.787	3.078	3.725
26	2.162	2.296	2.479	2.605	2.779	3.067	3.707
27	2.158	2.291	2.473	2.598	2.771	3.057	3.690
28	2.154	2.286	2.467	2.592	2.763	3.047	3.674
29	2.150	2.282	2.462	2.586	2.756	3.038	3.659
30	2.147	2.278	2.457	2.581	2.750	3.030	3.646
40	2.125	2.250	2.423	2.542	2.704	2.971	3.551
60	2.099	2.223	2.390	2.504	2.660	2.915	3.460
120	2.076	2.196	2.358	2.468	2.617	2.860	3.373
∞	2.054	2.170	2.326	2.432	2.576	2.807	3.291