

國立清華大學命題紙

99 學年度 動力機械工程學系乙組(電控組) 碩士班入學考試

科目 控制系統 科目代碼 0902 共 4 頁, 第 1 頁

\*請在【答案卷卡】作答

1. For the following system with input  $V_{in}$  and output  $T$  as shown in Fig. 1, (a) plot the block diagram and find the transfer function  $\frac{T(s)}{V_{in}(s)}$  (10%), (b) find the steady state response  $T(t=\infty)$  for a unit step input on  $V_{in}$  (5%)  
 (Assume the spin speed of the motor is so small that the back electromotive force  $e$  can be ignored.)

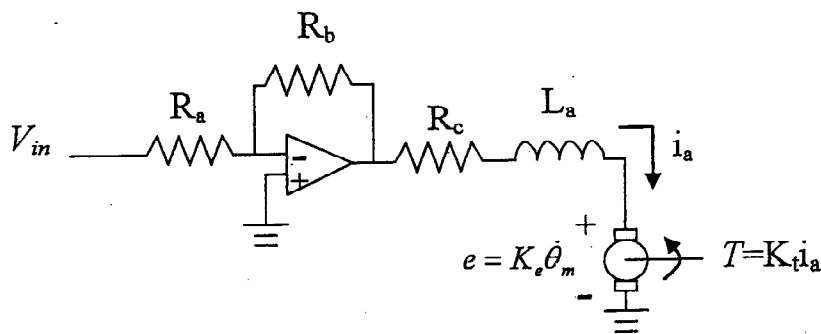


Fig. 1

2. For a system  $\frac{Y(s)}{R(s)} = \frac{4}{s^2 + 1.6s + 4}$ , the unit step response is shown as (a) in Fig. 2. Please relate curve (b), (c) and (d) to the unit step responses of the following systems. (10%)

(1)  $\frac{Y(s)}{R(s)} = \frac{-4s + 4}{s^2 + 1.6s + 4}$

(2)  $\frac{Y(s)}{R(s)} = \frac{4}{(s^2 + 1.6s + 4)(s + 1)}$

(3)  $\frac{Y(s)}{R(s)} = \frac{4s + 4}{s^2 + 1.6s + 4}$

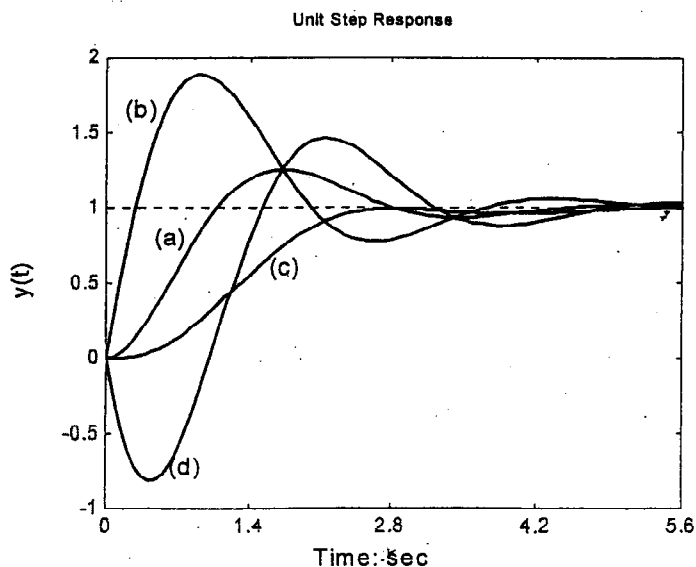


Fig. 2

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3. Consider the submarine depth control problem shown in Fig. 3 (a). The objective is to reach and maintain the desired depth. The submarine dynamics are given by  $G(s)$  (followed by an integrator), the stern plate actuator has a gain of  $K$ , and the dynamics of the pressure transducer is assumed to be very fast (namely,  $H(s)=1$ , as shown in Fig. 3(b))

- (a) Determine the range of  $K$  that will result in a stable closed-loop system. (10%)  
 (b) What is the closed-loop oscillation frequency (write down the unit) for marginally stable case? (10%)

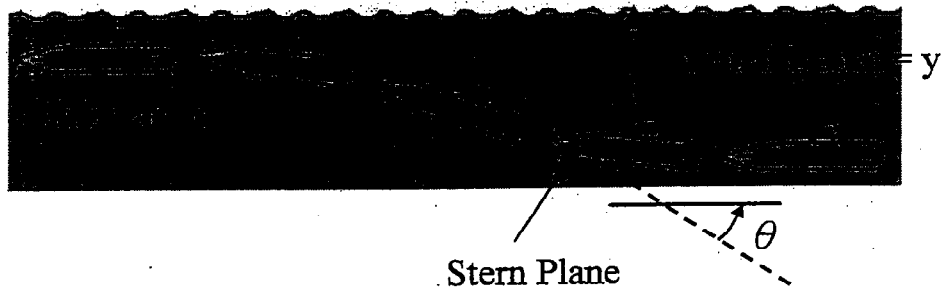


Fig. 3(a)

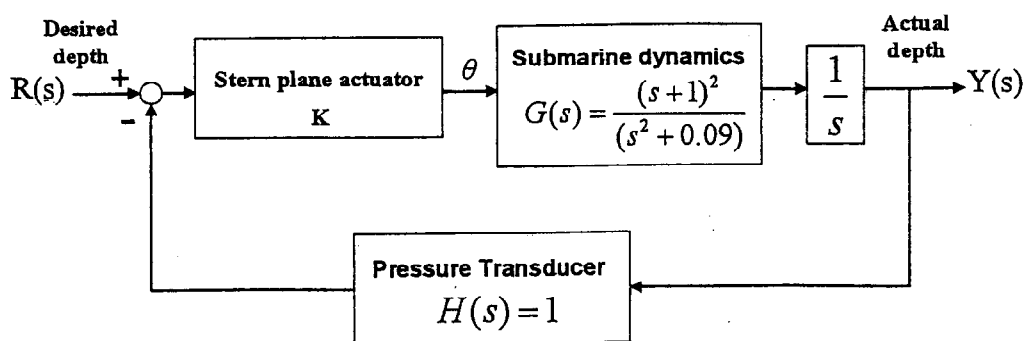
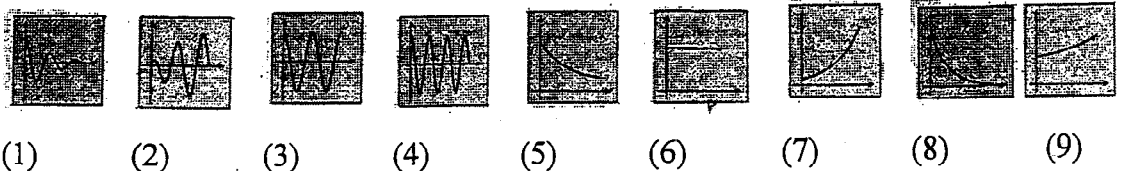
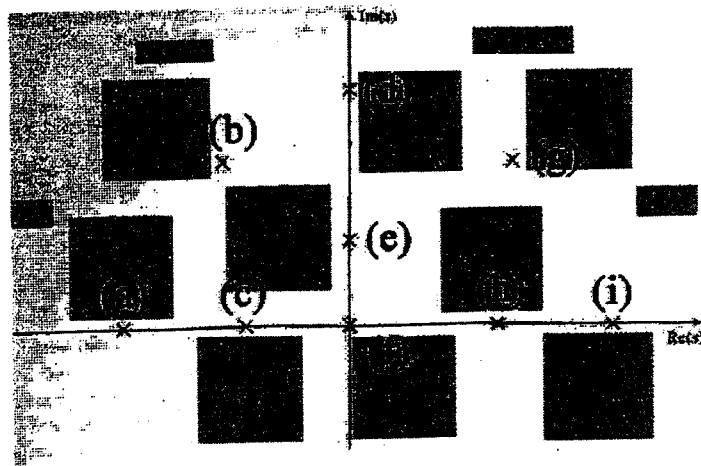


Fig. 3(b)

4. Please match the following impulse time responses (1)~(9) to the poles location (a)~(i). (5%; note: no partial credit)





5. Consider a system shown as Fig. 5, where  $G(s) = \frac{1}{(s+2)^2}$  and  $H(s) = \frac{1}{s+3}$

- (a) Sketch the root locus of the system when  $K$  varies from 0 to  $\infty$ . Be sure to give the asymptotes and the breakaway point. (10%)
- (b) If the system requires one pair of complex conjugate poles with real part equal to  $-1$ , determine the constant gain  $K$  and the corresponding system poles. (10%)
- (c) Design a phase lead compensator, i.e.,  $K = K_p \frac{s+Z}{s+P}$ , so that the system has one pair of complex conjugate poles with damping ratio  $\xi = \frac{2}{\sqrt{5}}$  and undamped natural frequency  $\omega_n = \sqrt{5}$ . (10%)

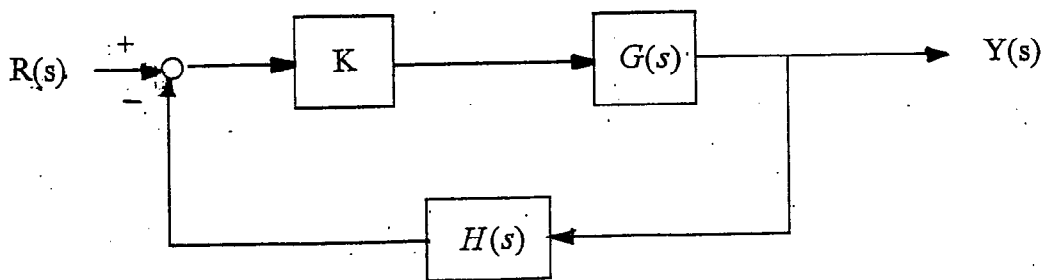


Fig. 5

6. A system is shown as Fig. 6(a), where  $G(s) = \frac{11}{s(s+10)}$  and  $H(s) = \frac{1}{s+1}$

- (a) Sketch the polar plot of  $G(s)H(s)$  and calculate the gain margin of the system if the closed contour of  $s$  is chosen as Fig. 6(b). (10%)
- (b) Determine the stability of the system by use of the Nyquist stability criterion. (5%)

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- (c) Sketch the Bode plot of  $G(s)H(s)$  and point out the gain margin and the phase margin of the system on your plot. (5%)

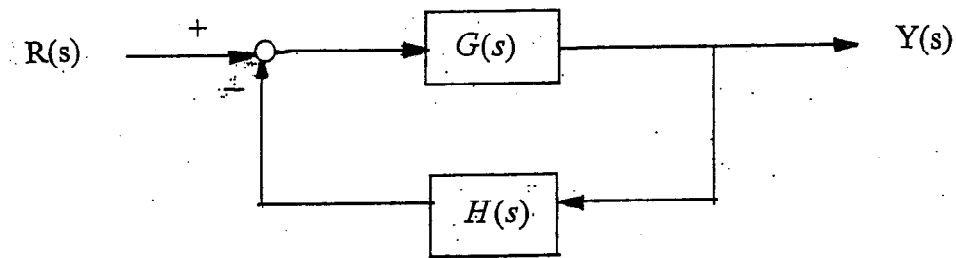


Fig. 6(a)

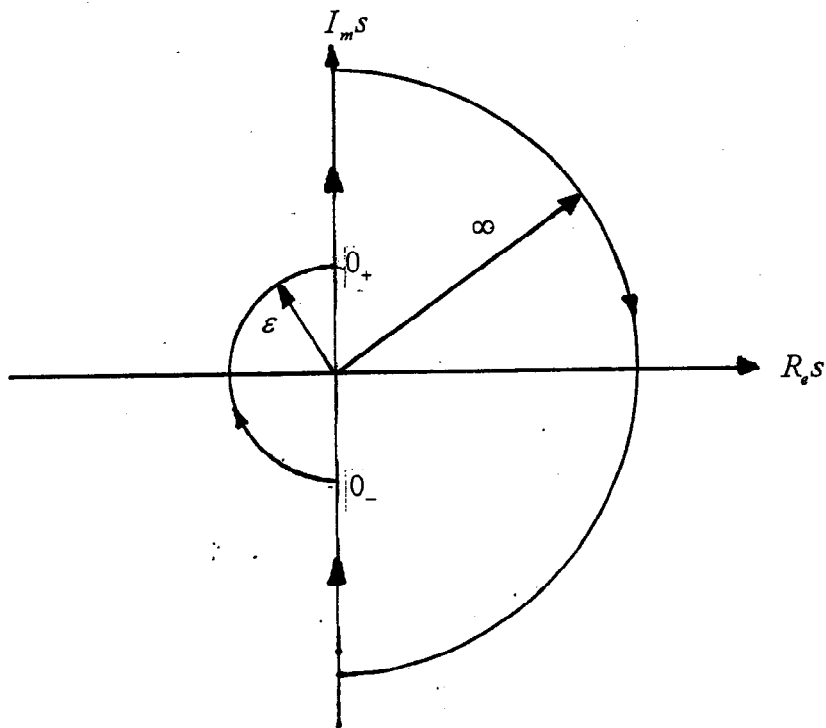


Fig. 6(b): Where  $\epsilon$  is very small.